


# Towards a fertility modifier for hybrid growth models

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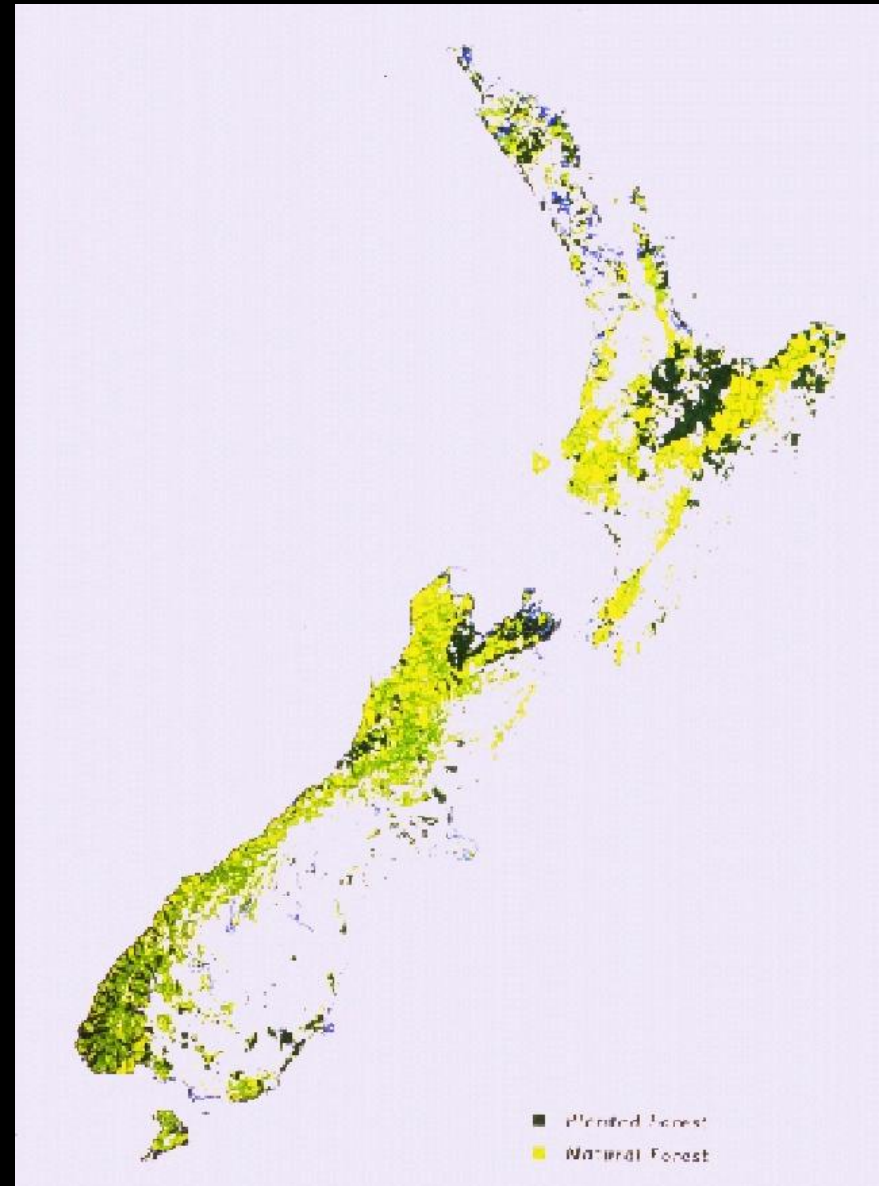


# Outline

- Introduction
  - Hybrid modeling
  - Phosphorus
    - Soil measurements
  - Nitrogen and Phosphorus
    - A simple approach
    - A step by step approach
- 

# New Zealand

- Current areas of Forest:
  - Indigenous - 6.3 million Ha.
  - Exotic (mostly *P. radiata*) - 2 million Ha.
  - 27% of NZ
- Much P deficiency





# P deficiency



# An example “hybrid” model

3-PG Model (Landsberg & Waring 1997)

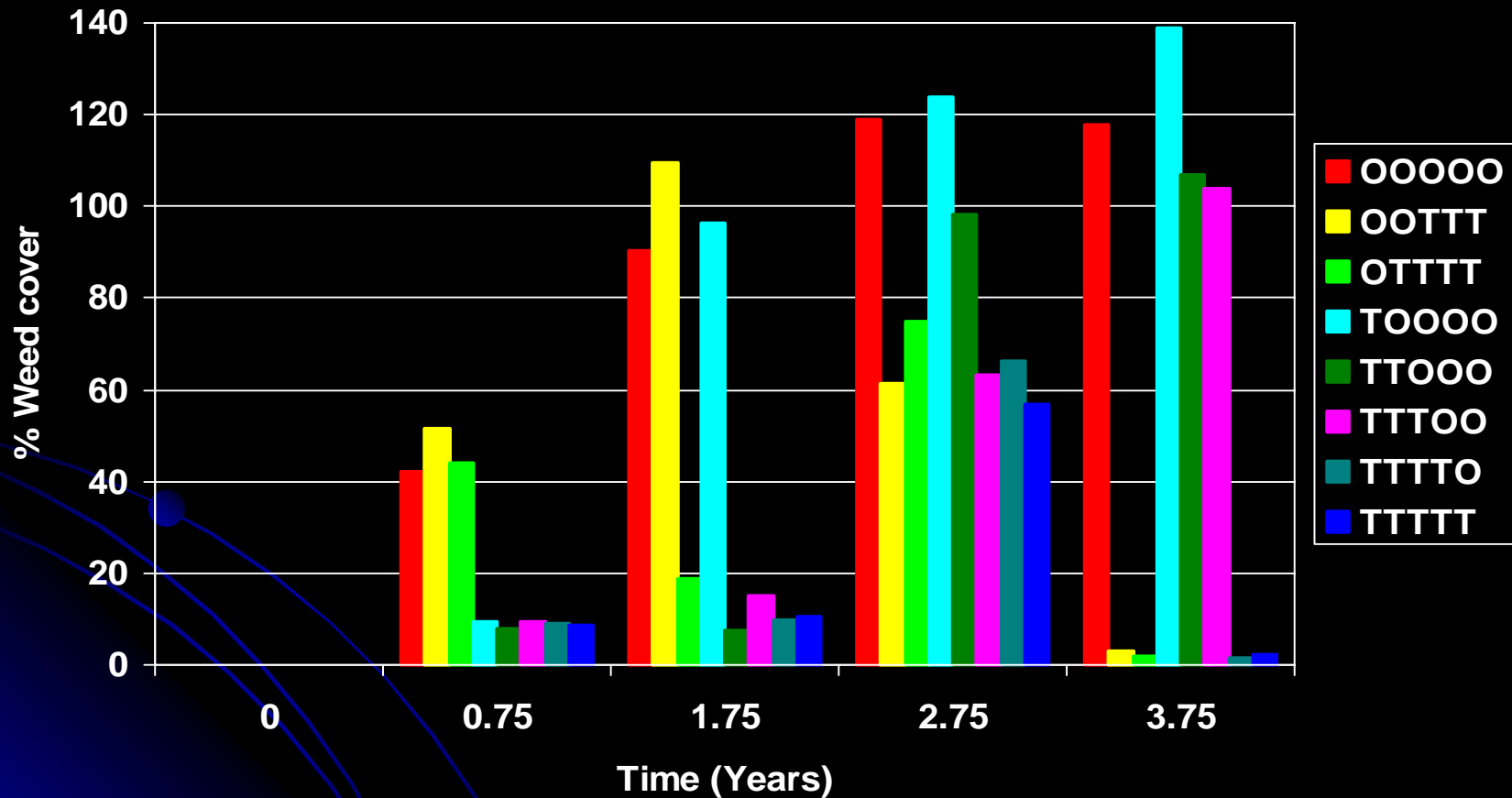
$$NPP = \varepsilon \sum_{t=1}^t APAR_t \min[f_{\theta} f_D] f_T f_F f_S$$

Allocation varies with fertility

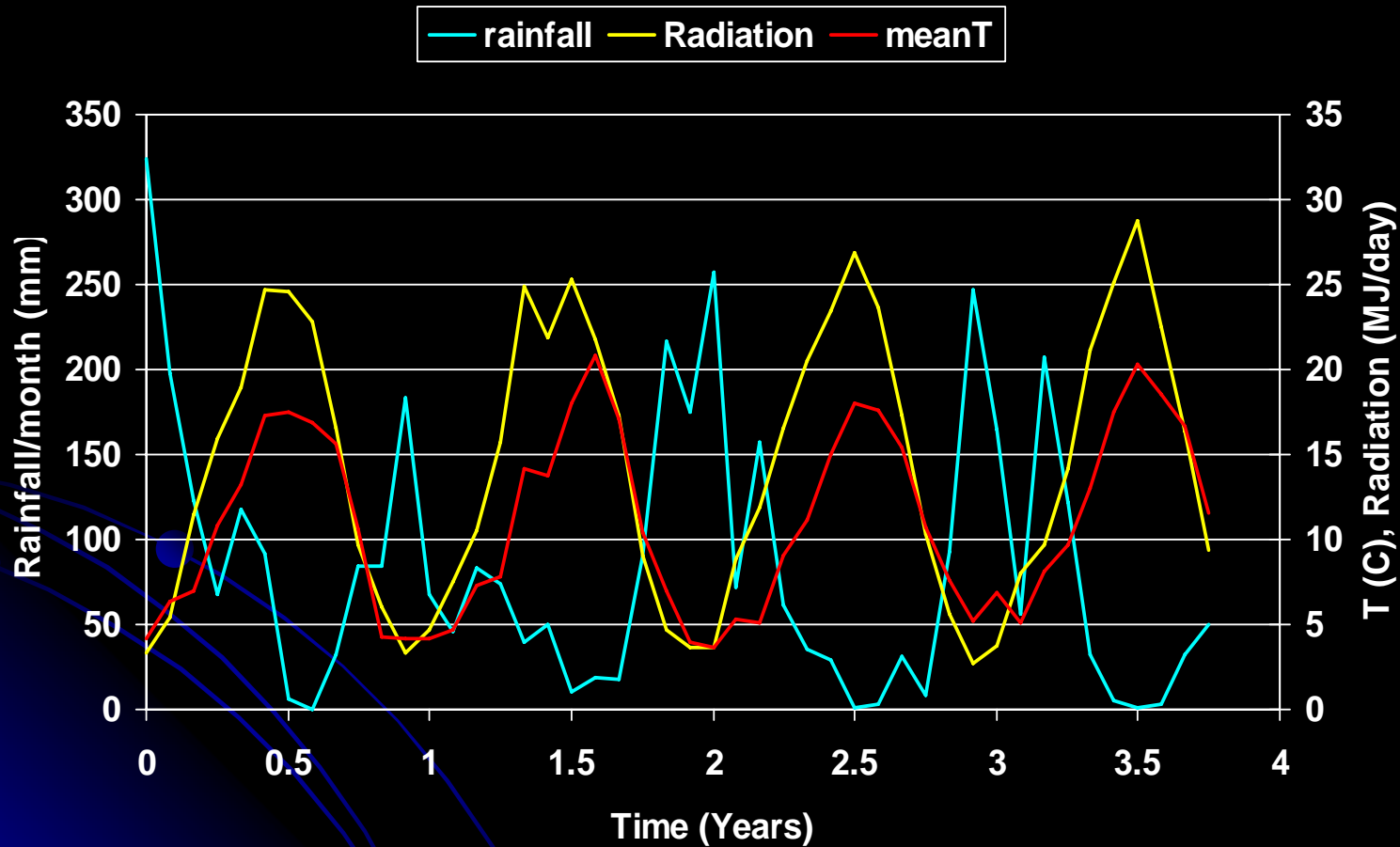
# Starker CPT study



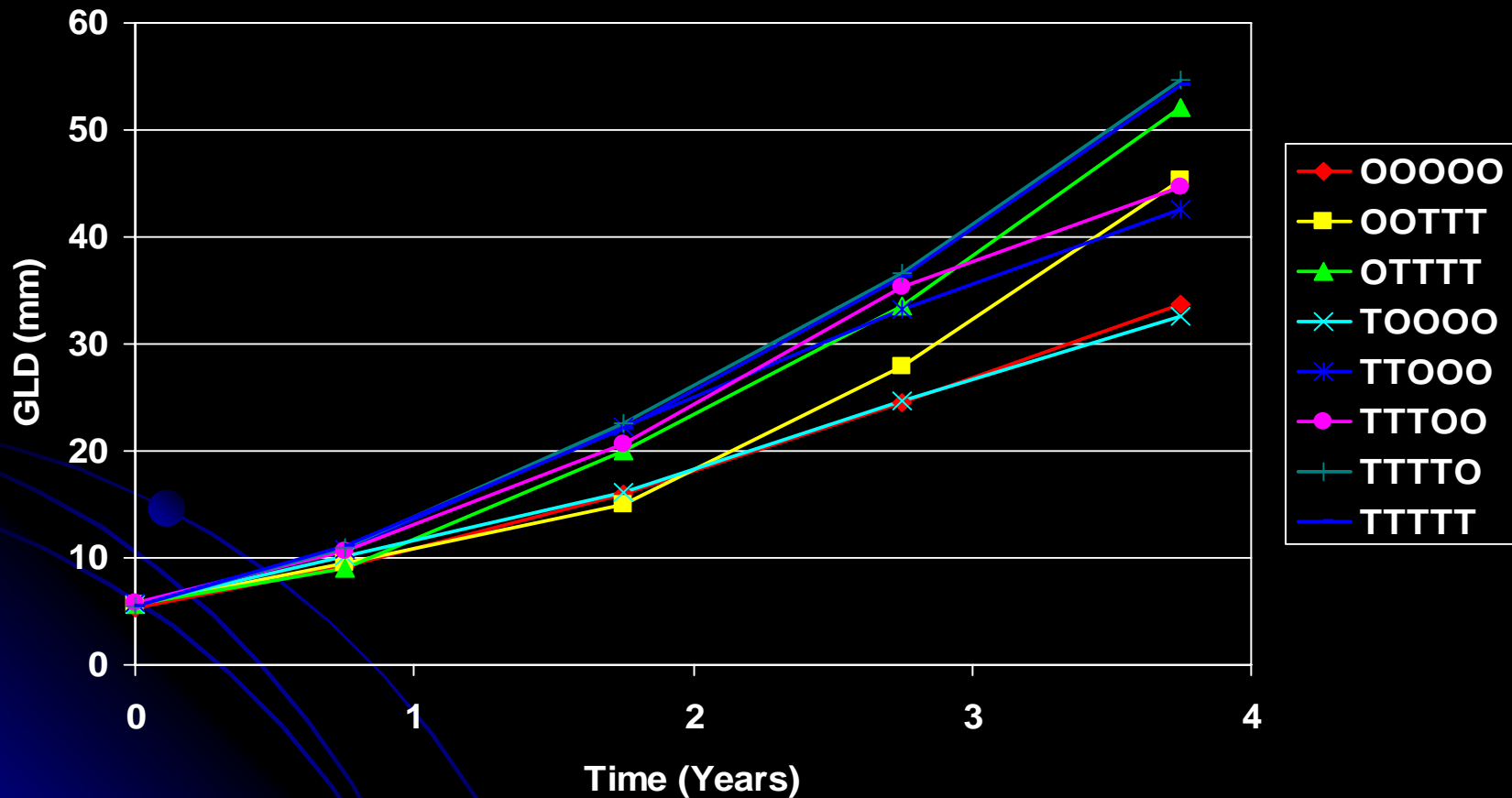
# Estimated weed cover within 2 m diameter zones around trees



# Climate by month

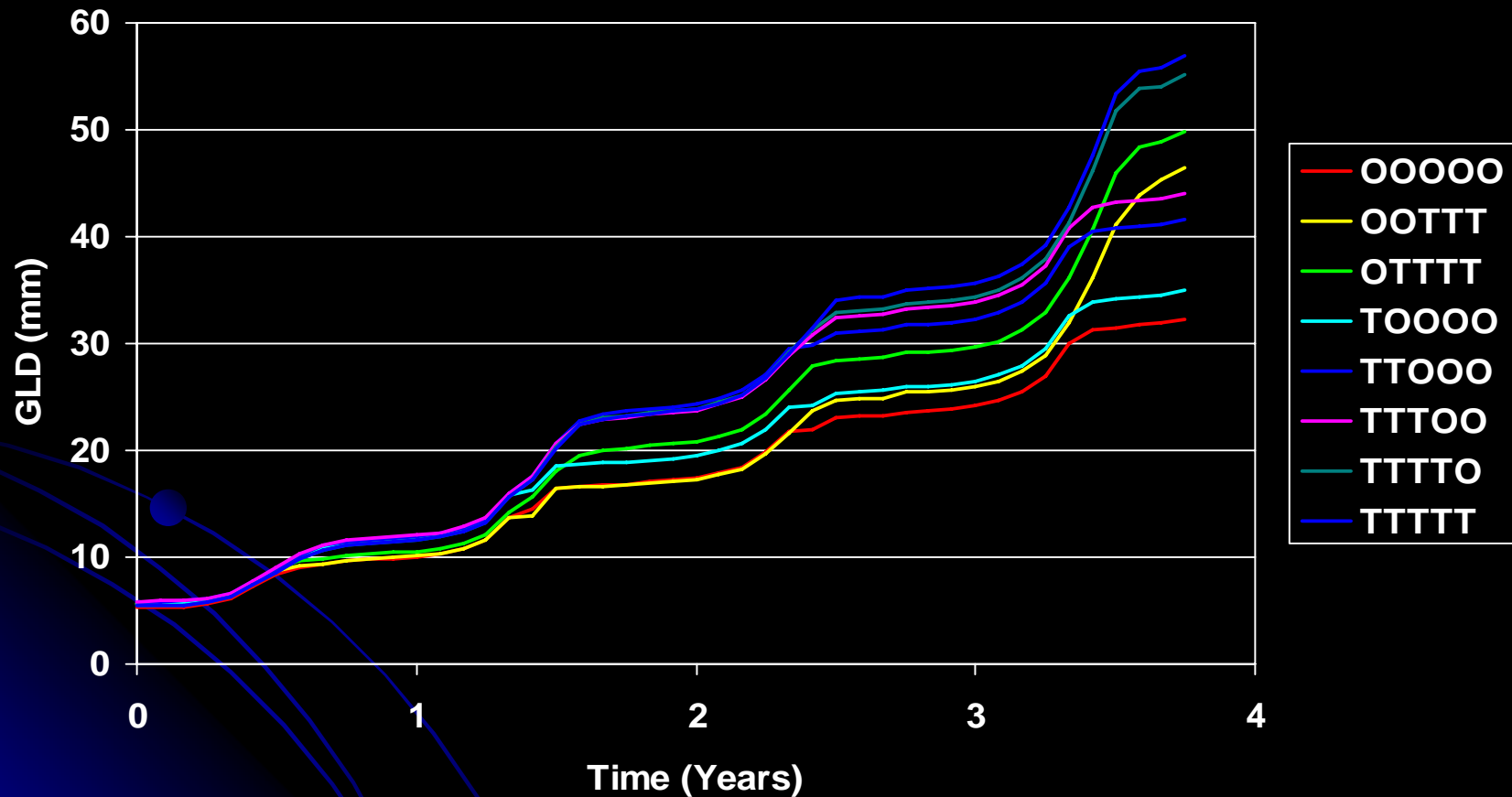


# Observed Ground Line Diameter

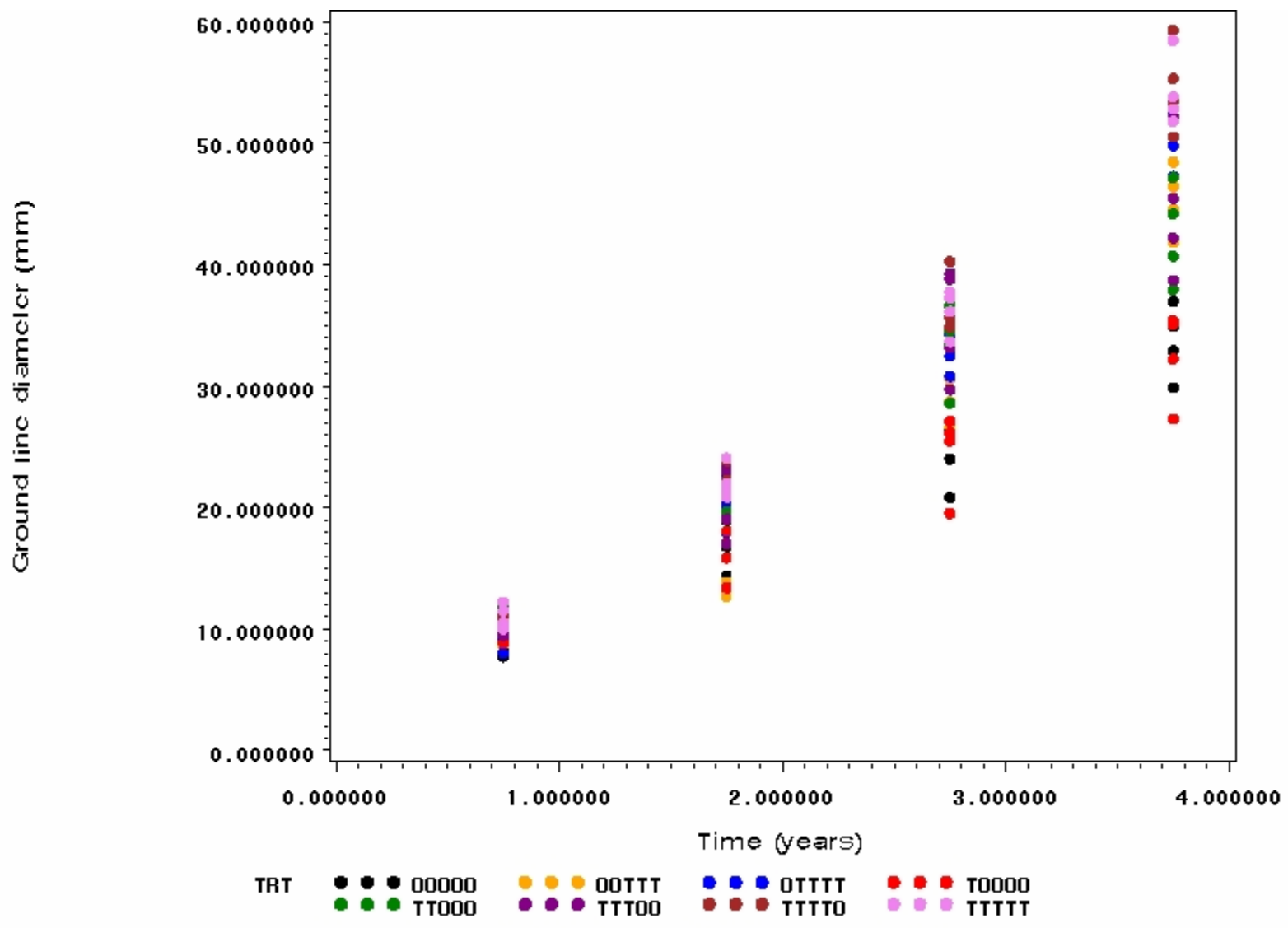


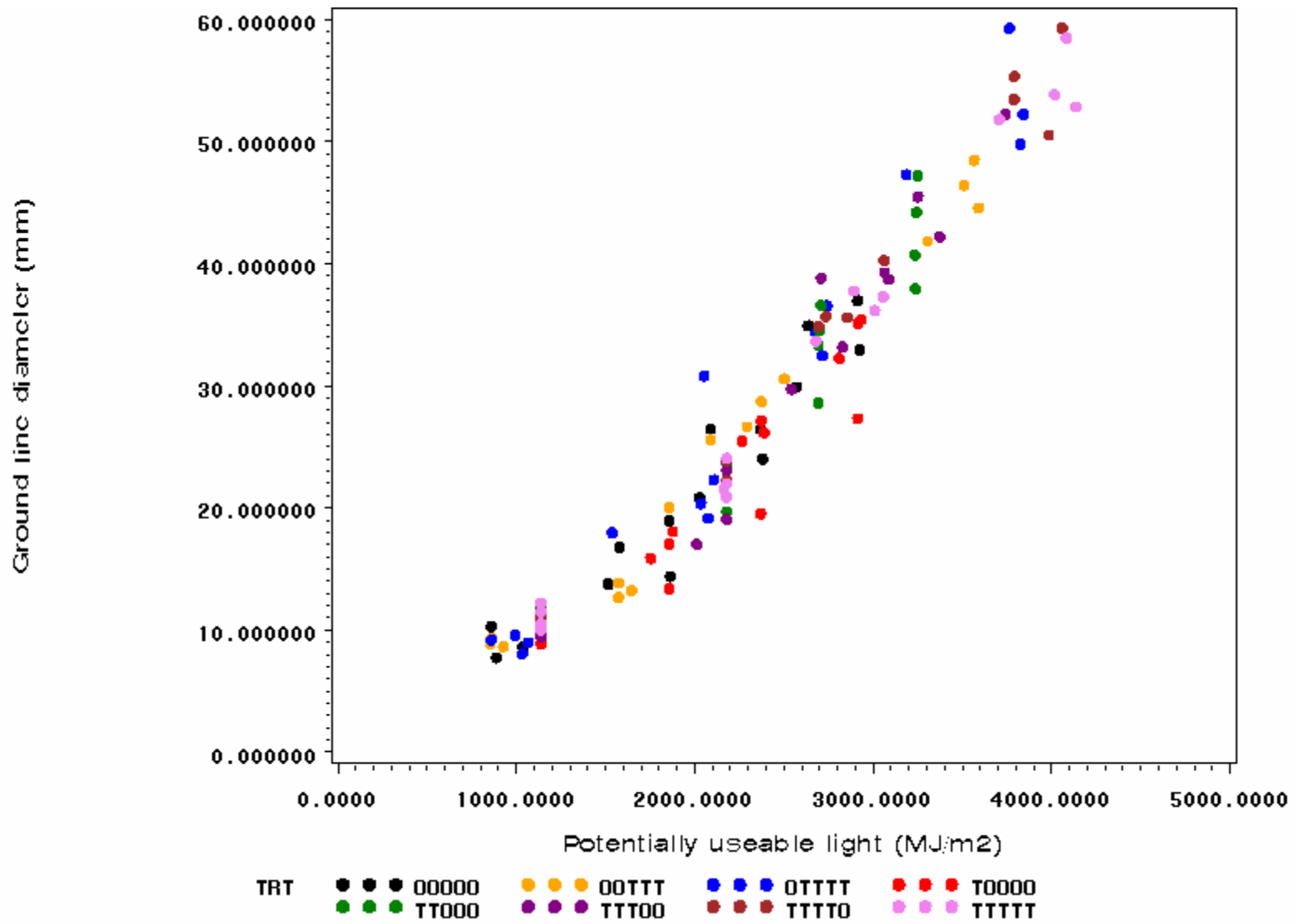
N.B.: Analysis of Douglas fir only

# Modeled ground line diameter



N.B.: Analysis of Douglas fir only





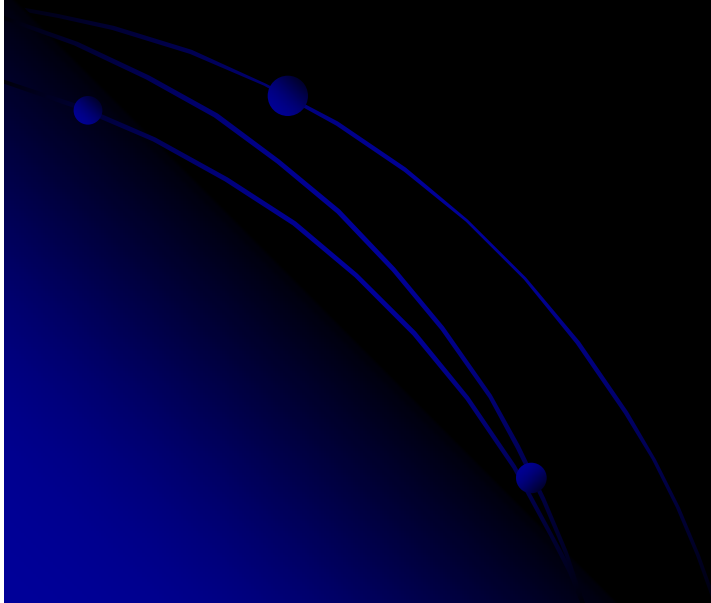
## Model form

$$Y_T = Y_0 + \alpha R_T^\beta$$


$$R_T = \sum_{t=1}^t R_t f_T \min[f_D f_\theta]$$

Summed across months

What kinds of sub-models are needed to represent fertility in hybrid models?



# Overview

- Demand
    - Nutrient assays
    - Understanding of processes
  - Supply
    - Weathering
    - Rainfall
    - Mineralisation
    - Retranslocation
- 

# 1. Soil measurement of P deficiency – with Malcolm Skinner

- Bray P
  - Immediate supply
- Release from weathering can be significant
- Hypothesis
  - Response to P fertilisation will be correlated with both immediate supply and weathering
  - Repeated extractions from the same soil sample can mirror weathering

# Methods

- 35 experiments throughout New Zealand
- N \* P factorial
  - Sometimes site preparation was a factor
- N+P contrasted with no fertilisation
- Height and gld measured at age 4
- Soil samples
  - Depth 0-10 cm
  - Ten Bray P extractions from each

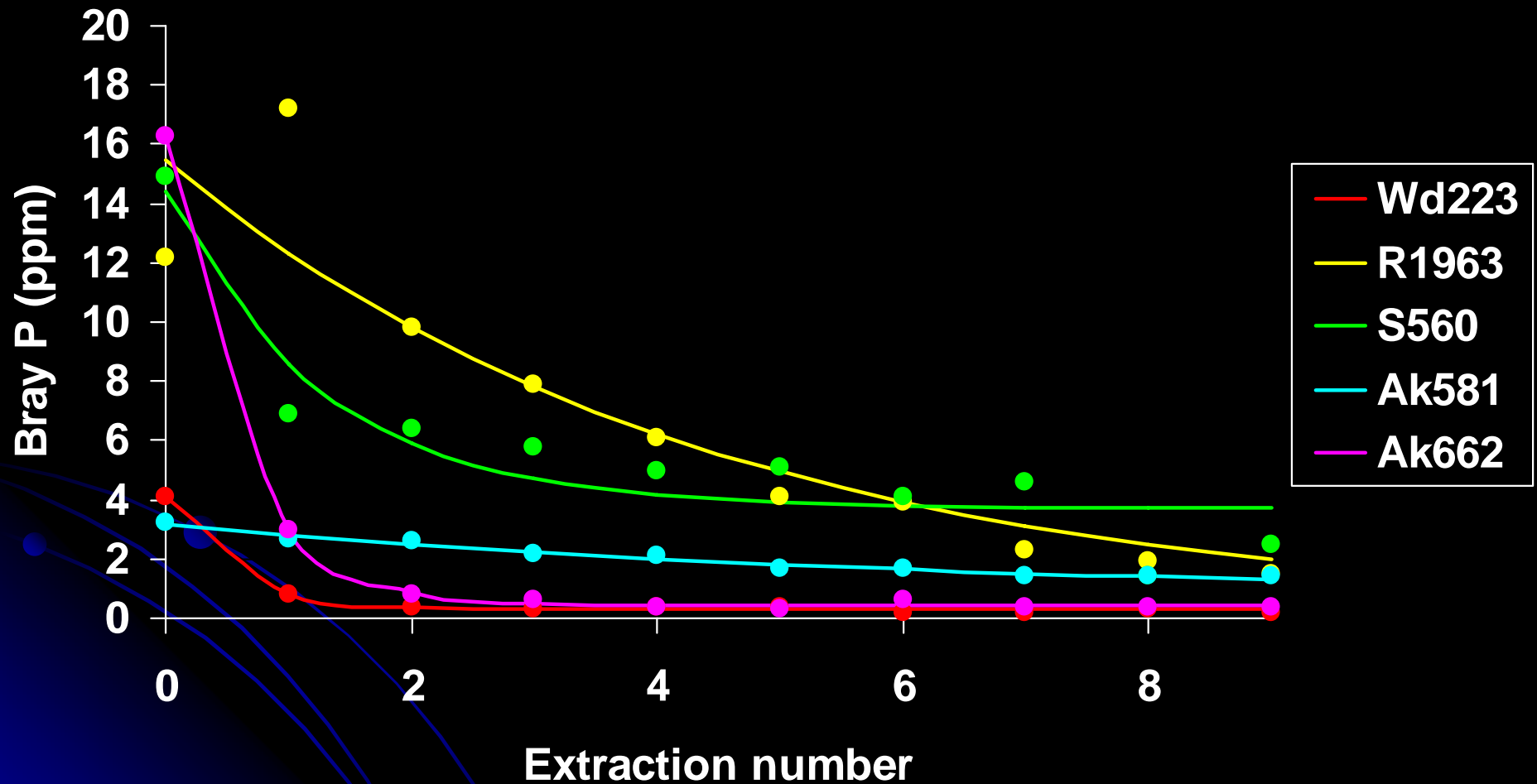
# Methods

- Exponential decay fitted to extractions

$$BrayP = \beta + (\alpha - \beta)e^{-\gamma N}$$

- N=extraction numbered from 0-9
- Response represented as a ratio of d<sup>2</sup>h
  - No fertilisation / fertilisation
- Response to P regressed against coefficients from exponential equation
- Effect of number of extractions tested

# Results – example fits



Measured fertility ratios : 0.02 0.87 0.64 1.00 0.04

# Results – Fertility ratio (FR)

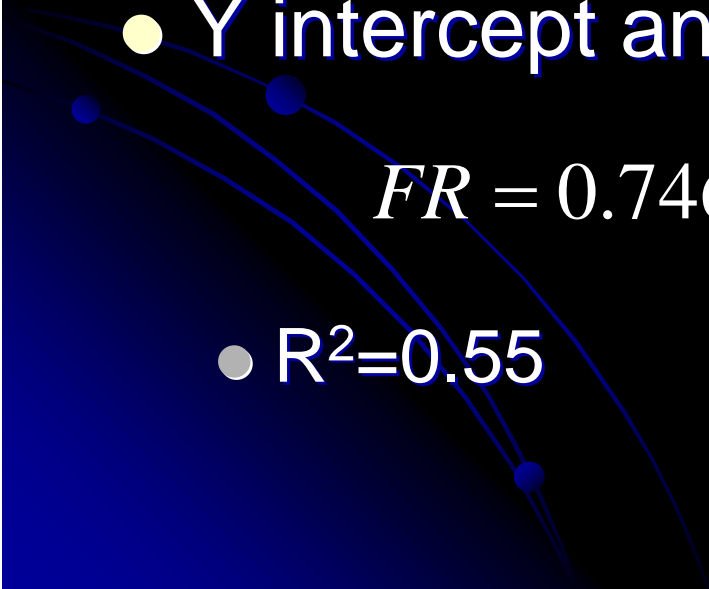
- First Bray P only

$$FR = m * BrayP + b$$

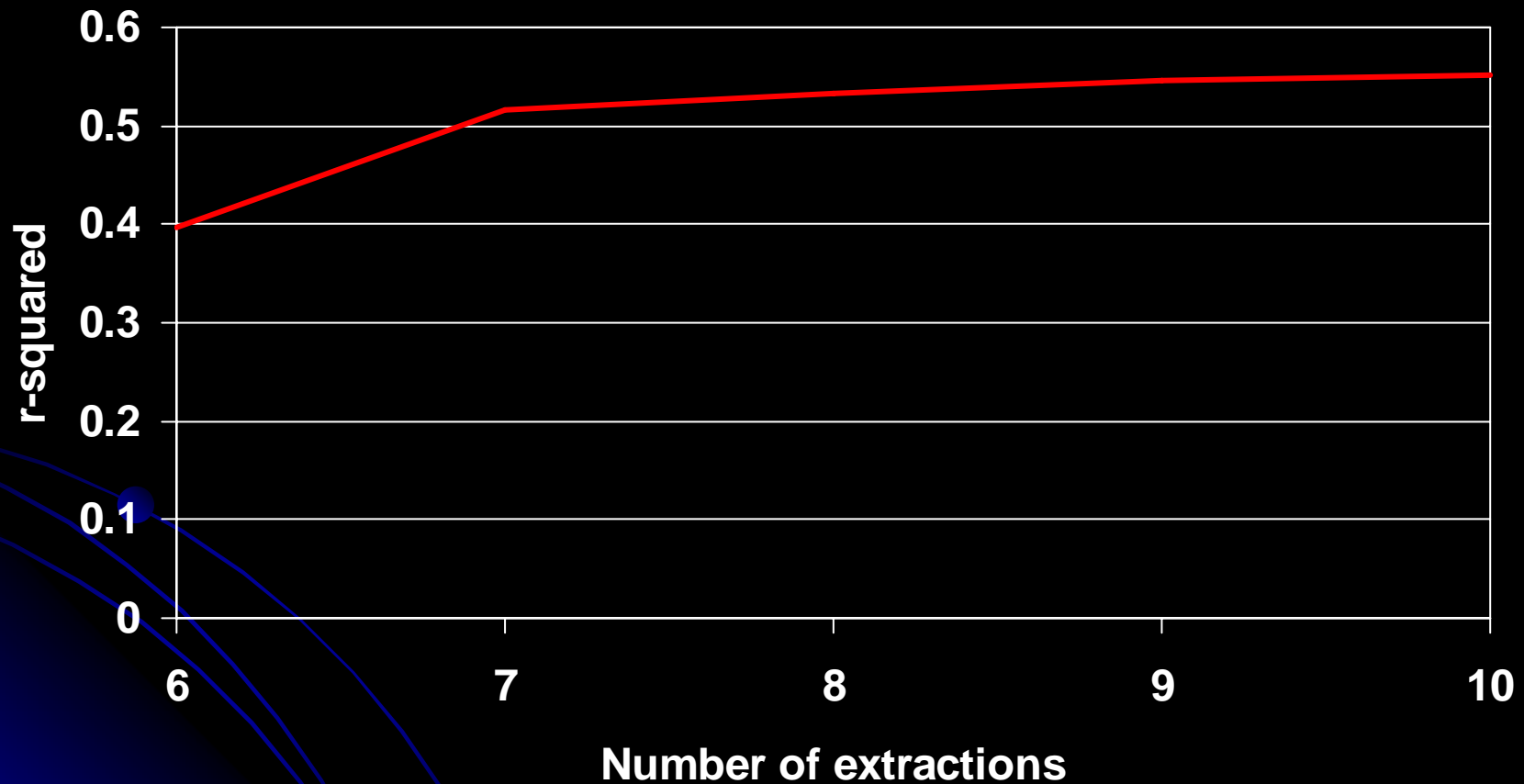
- $R^2=0.24$

- Y intercept and concavity of exponential

$$FR = 0.7466 - 0.3926\gamma + 0.0124\alpha\gamma$$

- $R^2=0.55$
- 

# How many extractions?



# Cautions

- Ratio is of stem measurements
  - Allometry changes with plant size
  - Allocation  $\neq$  allometry
- No account of changes in C allocation to roots with fertility
  - Assumed with 3-PG
- Represents P only

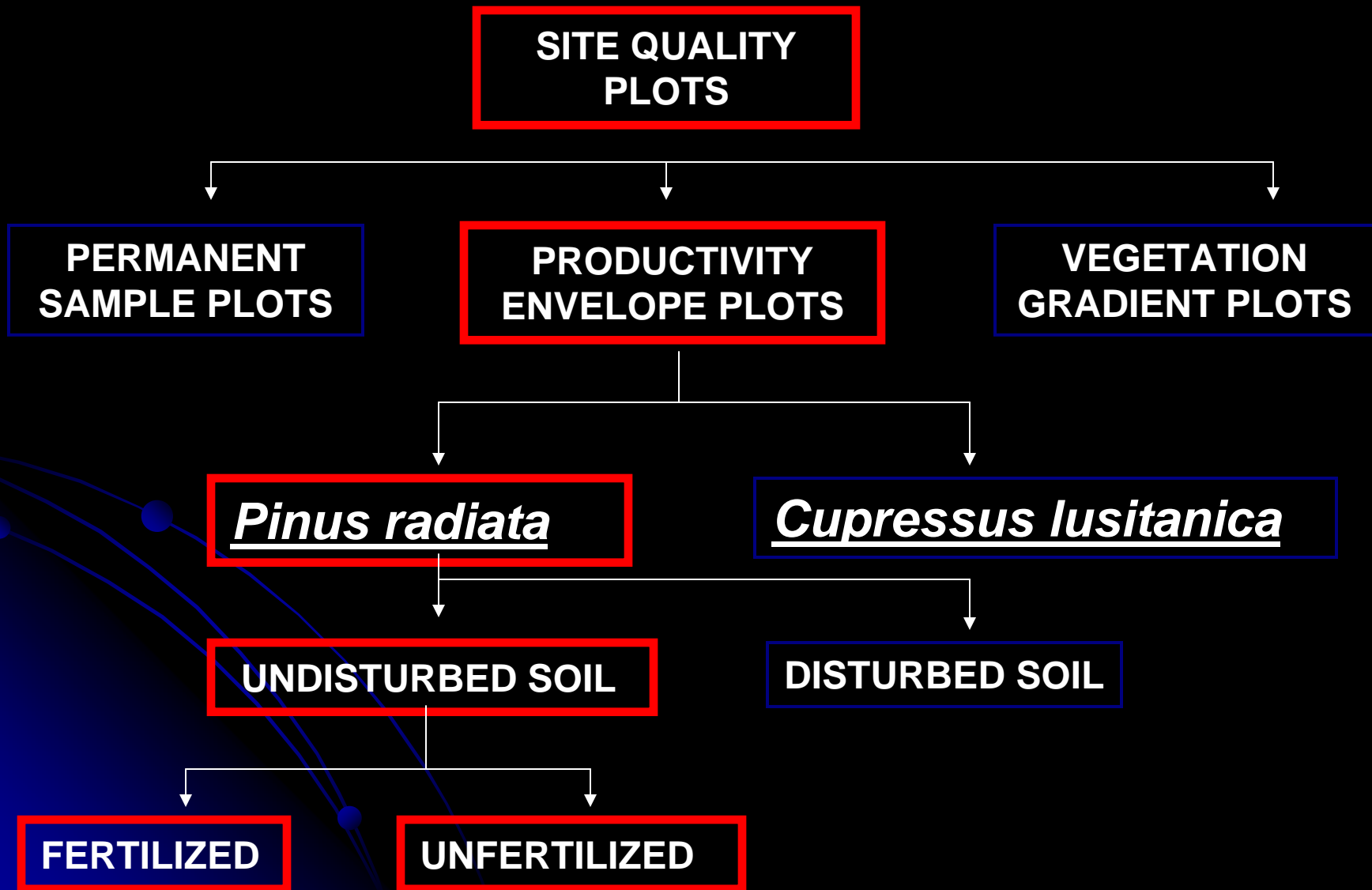
## 2. N, P & C:N ratio

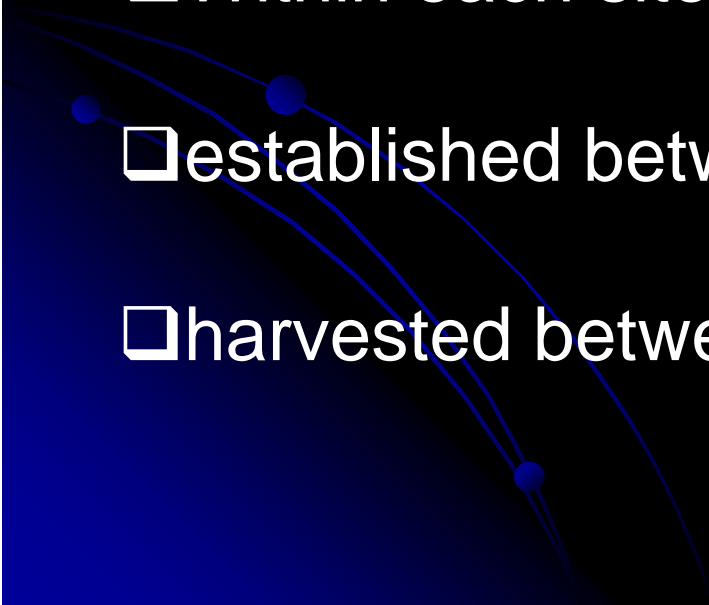
with Horacio Bown, Peter Clinton, Mike Watt &  
Brian Richardson

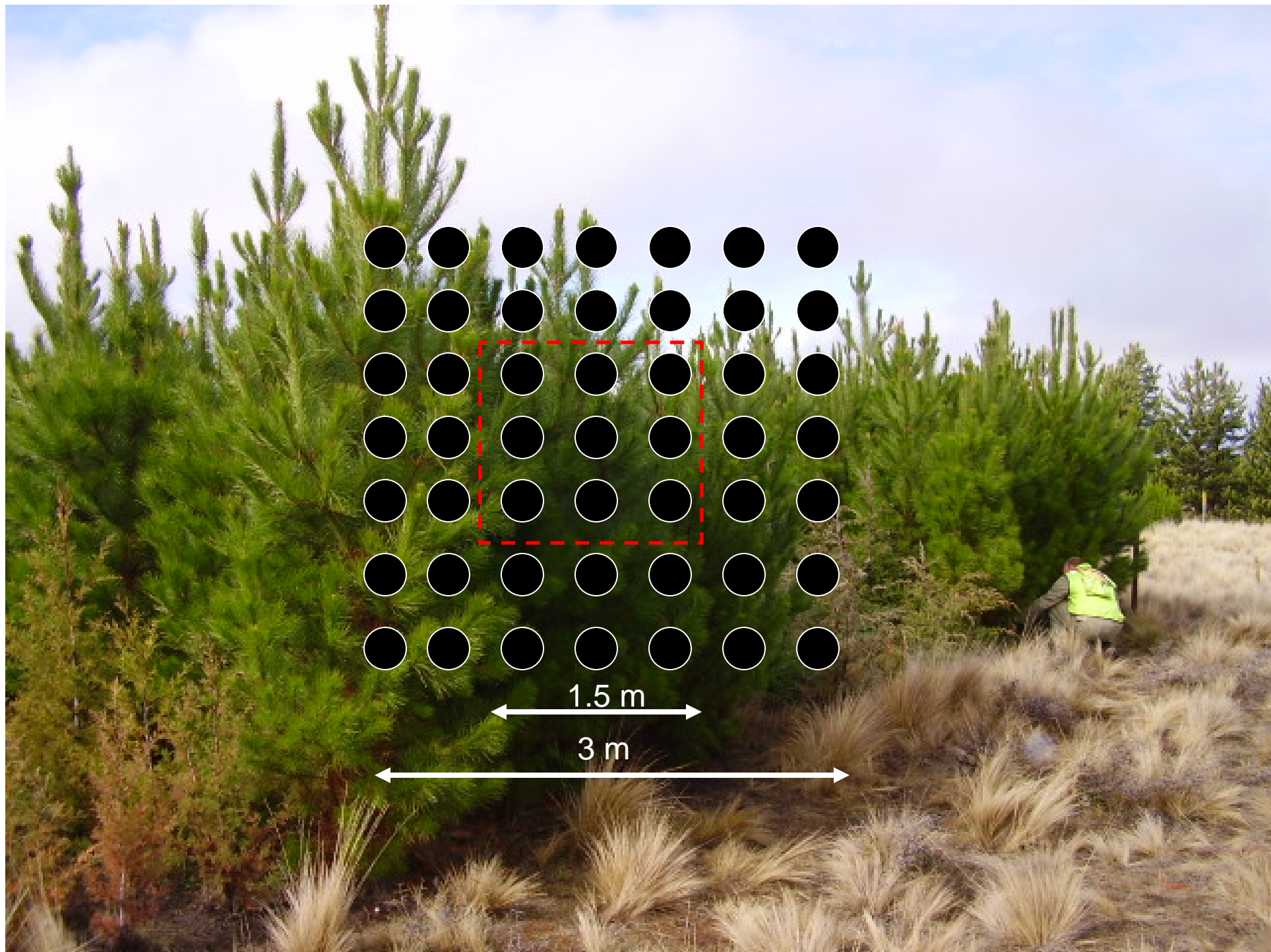
- N is sometimes critical in NZ
- N:P ratio may be significant
- Form of N can affect results
- Retranslocation must be accounted for
- Simple vs step by step approaches



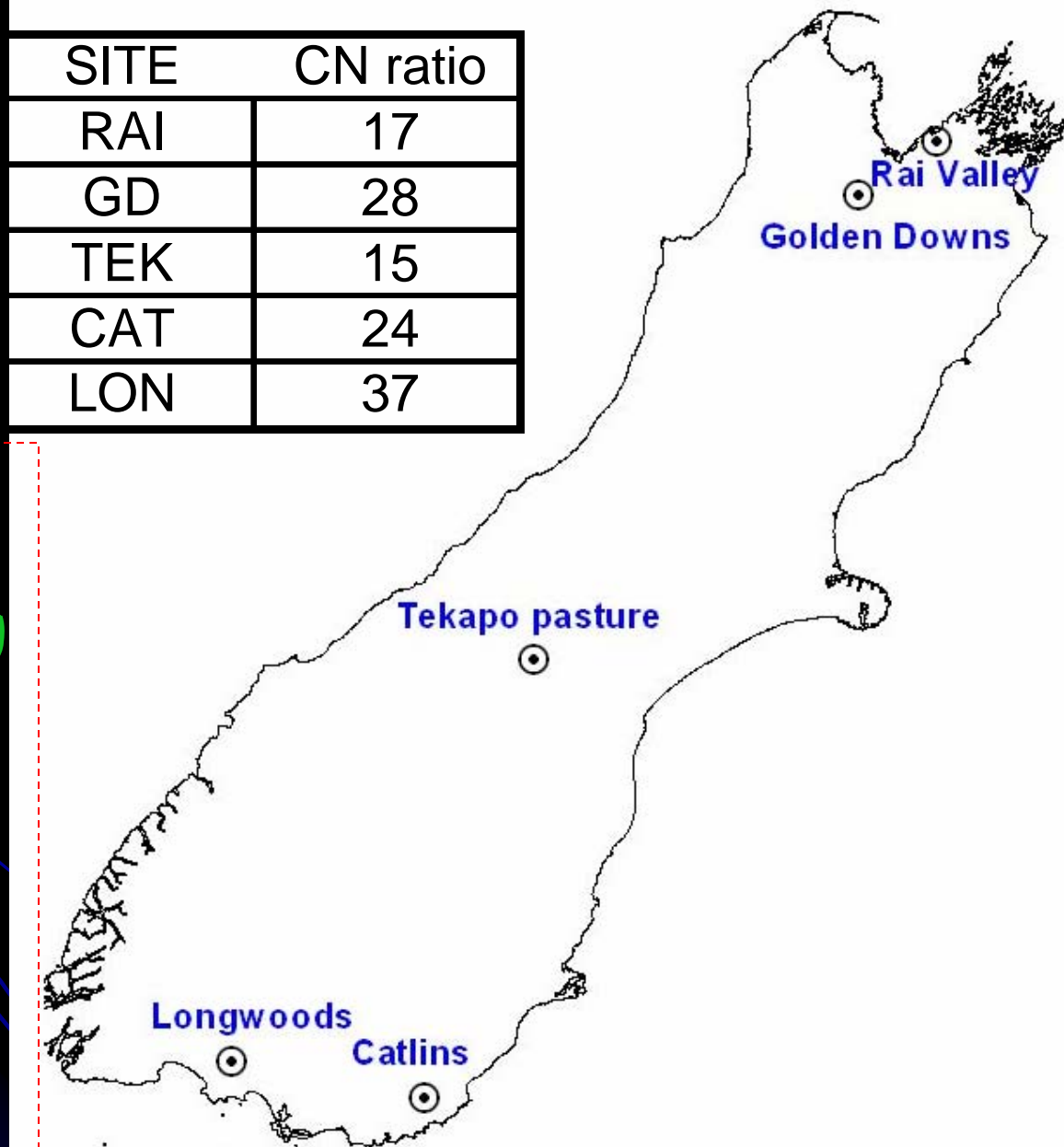
# A simple approach



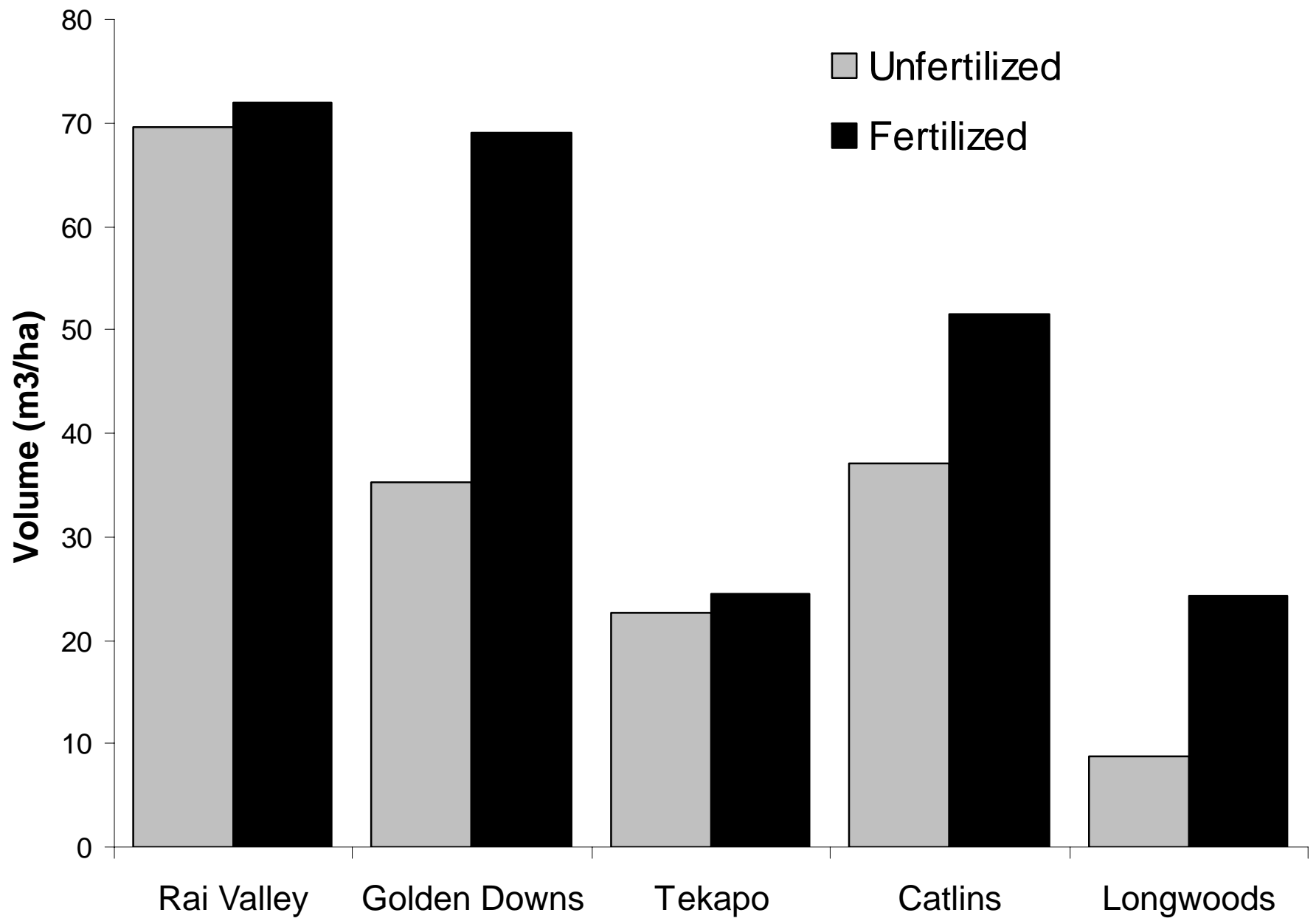
- ❑ Site quality plots comprise 35 sites across NZ
  - ❑ 5 sites selected for the purposes of the study
  - ❑ selected within the SI to cover gradient fertility
  - ❑ Within each site 2 plots were selected
  - ❑ established between July and September 2001
  - ❑ harvested between August and September 2005
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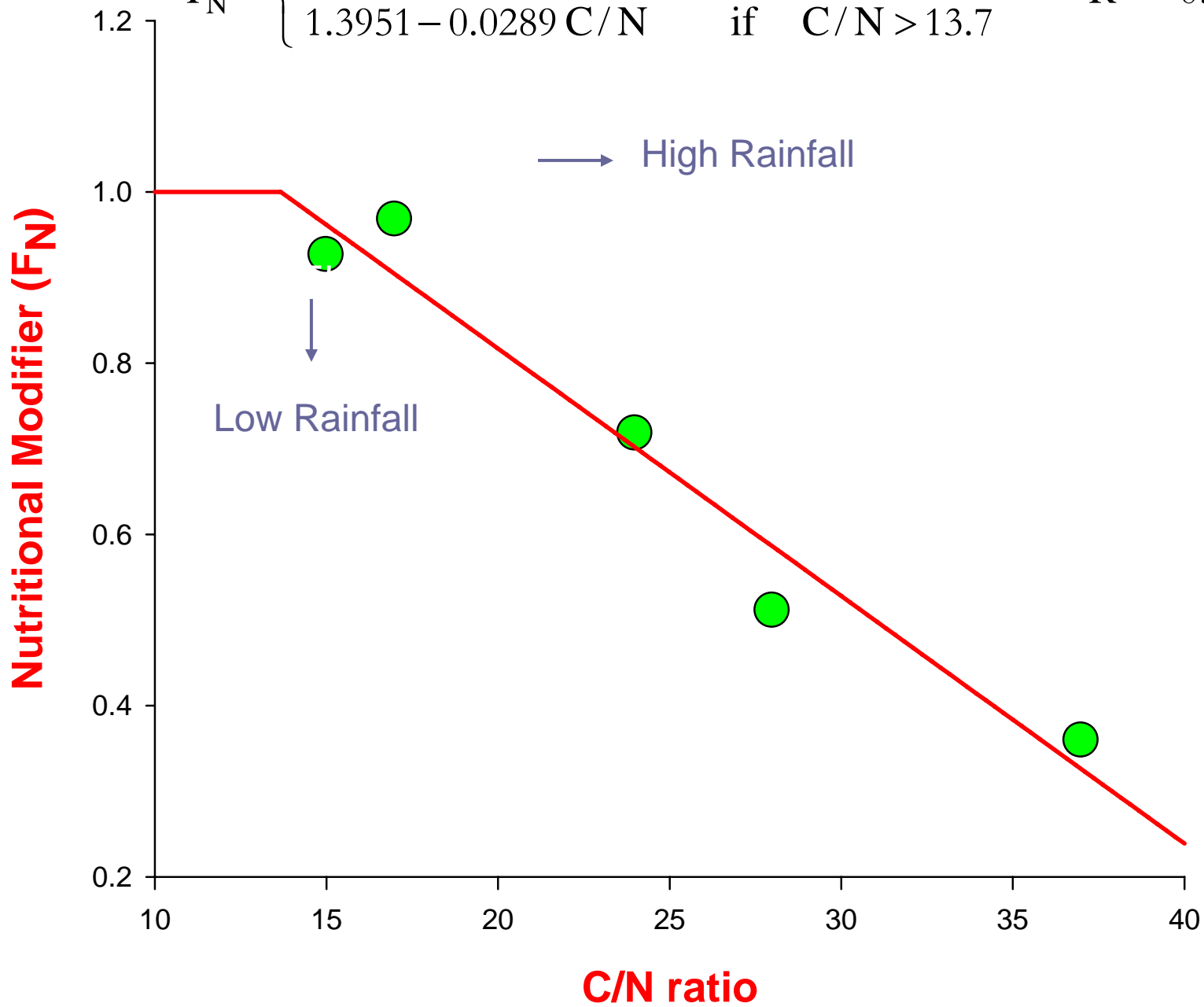
SITE	CN ratio
RAI	17
GD	28
TEK	15
CAT	24
LON	37



Horacio & Mike visited all 5 sites 12 times over a year. 12 trips of 2,500 km, or 30,000 km = return ticket to South America !!!!



$$F_N = \begin{cases} 1 & \text{if } C/N \leq 13.7 \\ 1.3951 - 0.0289 C/N & \text{if } C/N > 13.7 \end{cases} \quad R^2 = 0.95$$

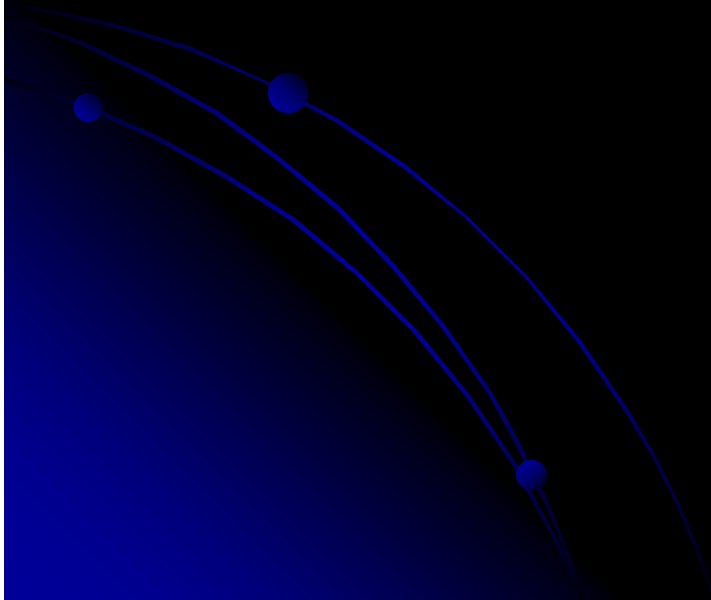


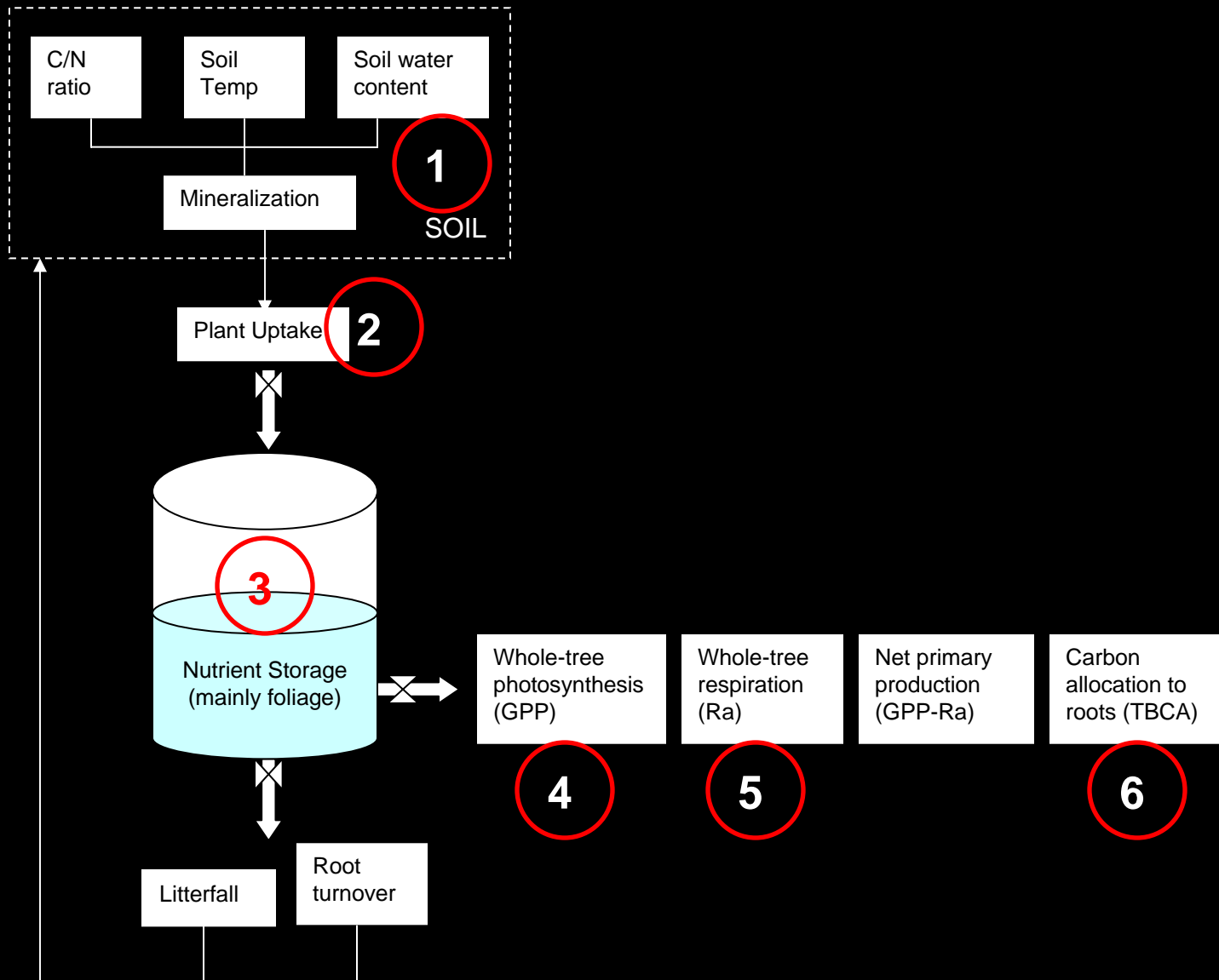
# Advantages of simple approach

- Simple to use
- Physiologically sound?
- In the short run, you would expect interaction between water and nutrient availability
- In the long run, the interaction can be neglected (Compare Rai valley and Tekapo)
- Fertilization can be easily handled as a reduction in the C/N ratio

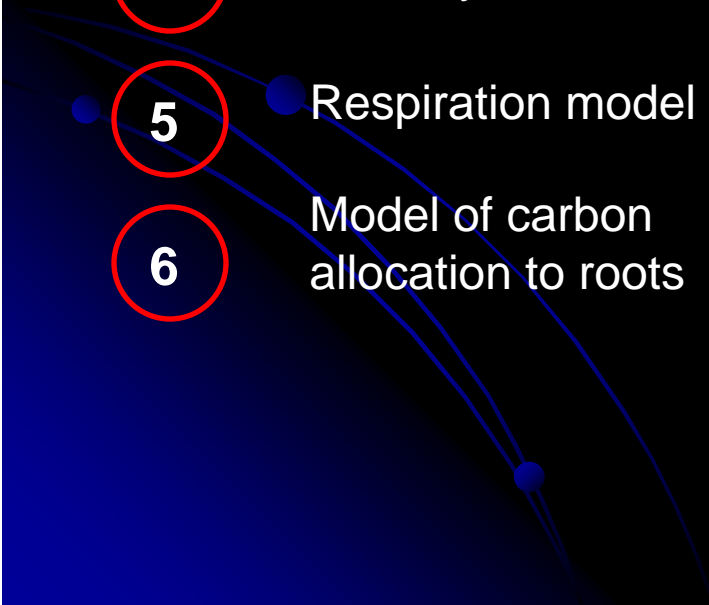
# A step-by-step approach

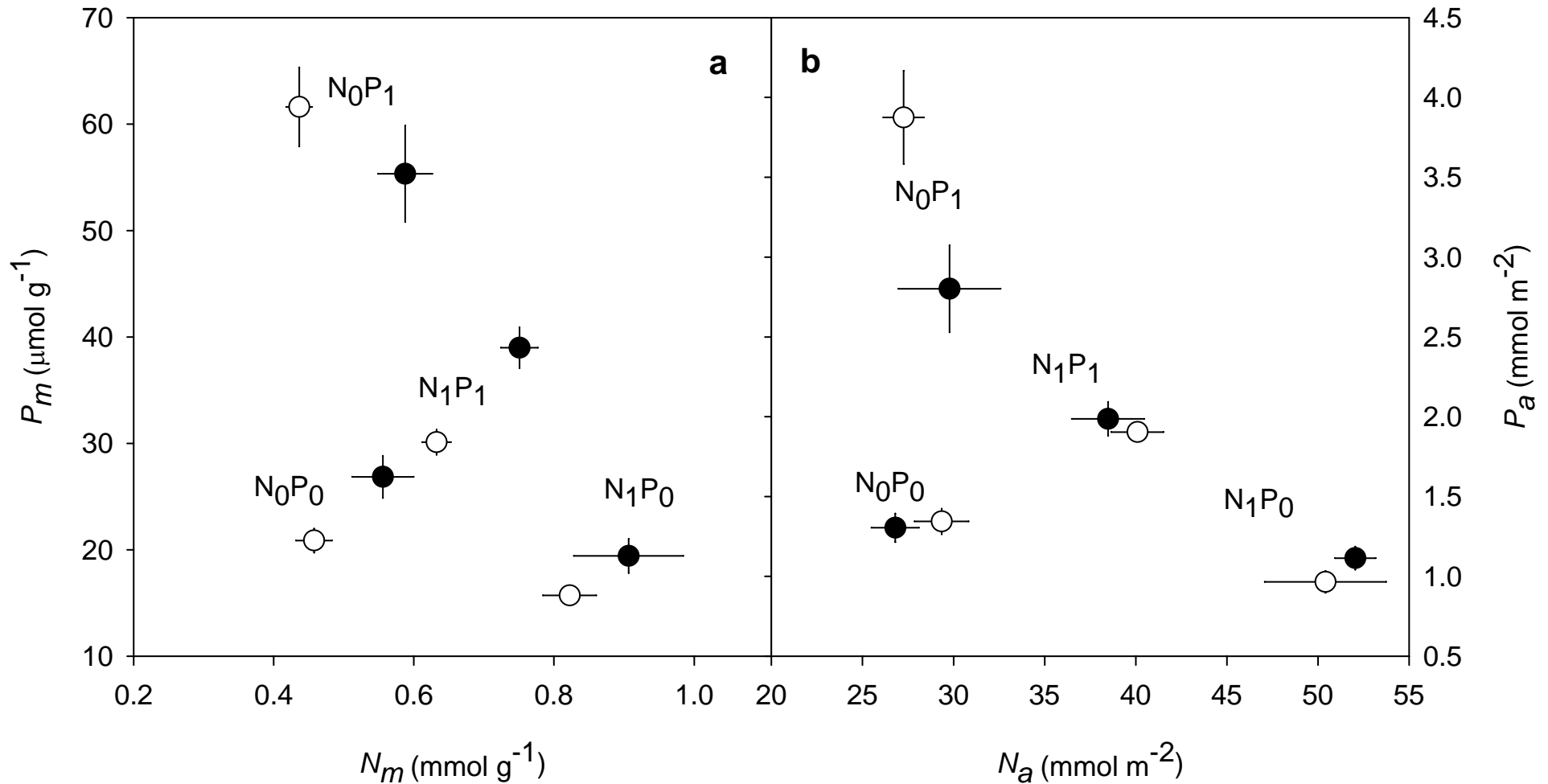
1. Construct a nutrient balance model
2. Drive photosynthesis and carbon allocation on a monthly step



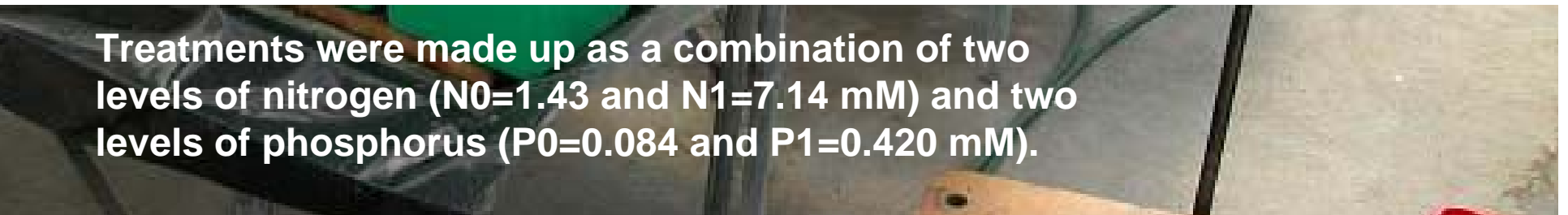


# Field and glasshouse studies

- 1 Soil mineralization model → Field
  - 2 Tree uptake model → Field
  - 3 Storage and Retranslocation model → Glasshouse & Field
  - 4 Photosynthesis model → Glasshouse
  - 5 Respiration model → Glasshouse
  - 6 Model of carbon allocation to roots → Glasshouse & Field
- 

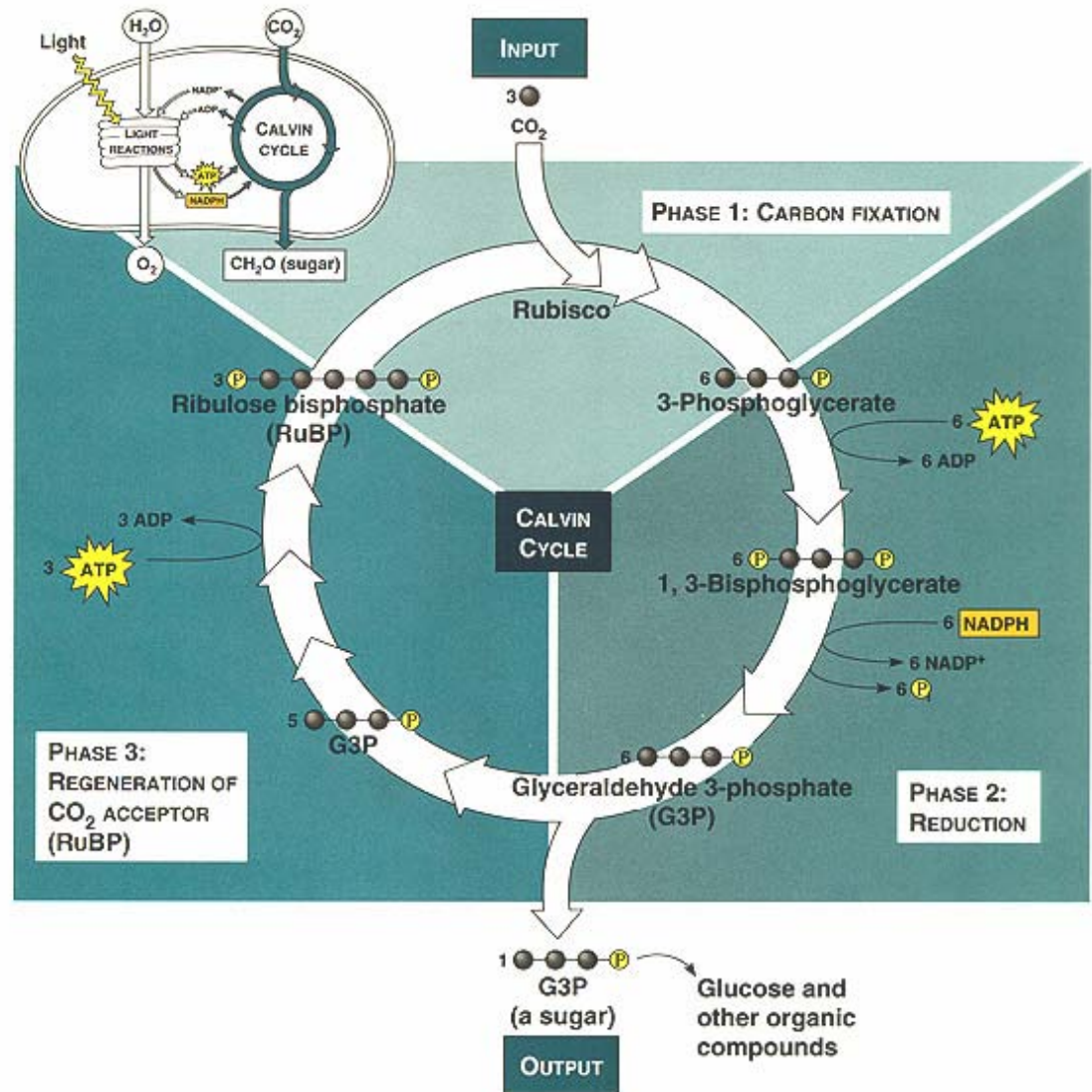


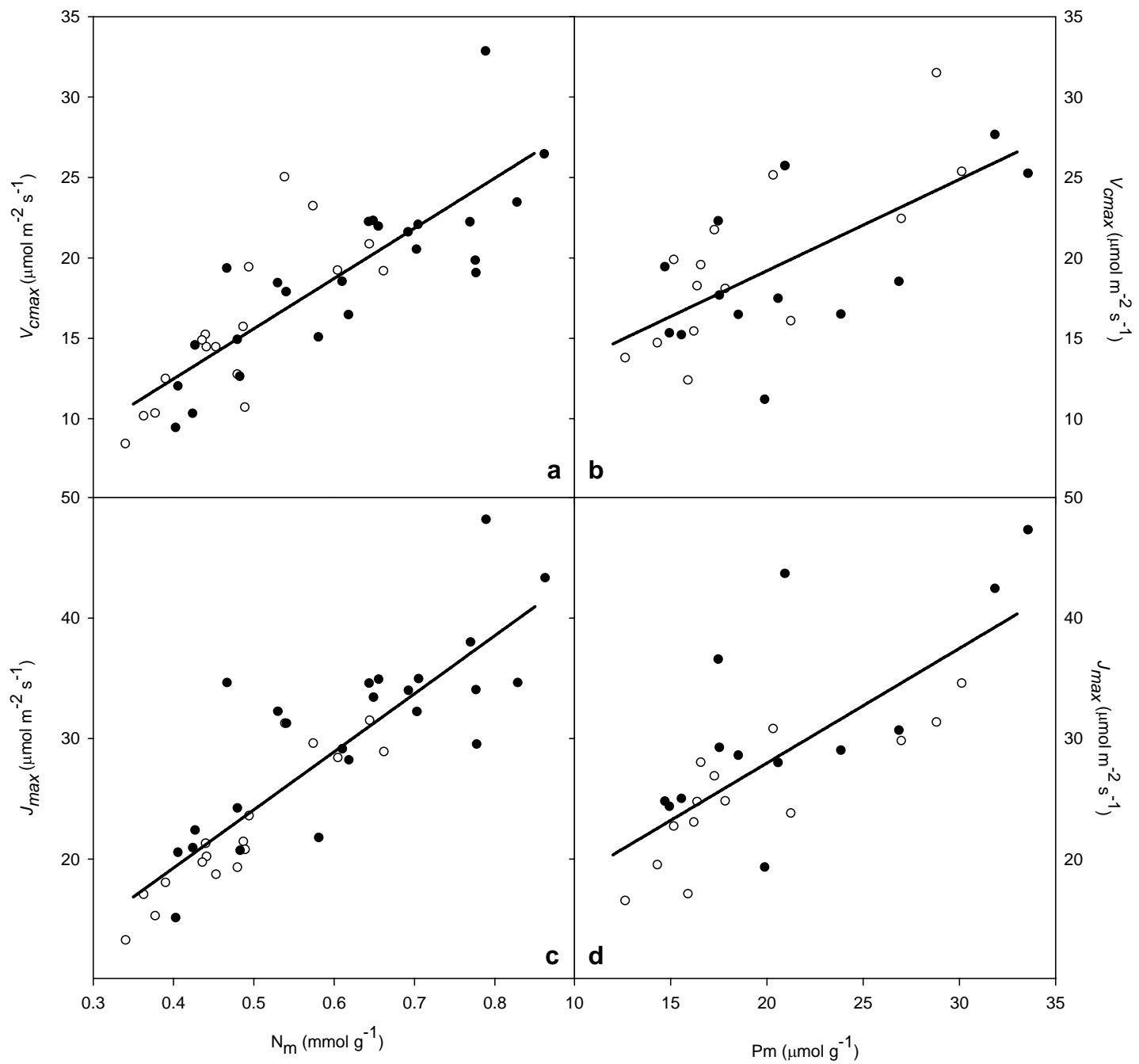
Treatments were made up as a combination of two levels of nitrogen (N<sub>0</sub>=1.43 and N<sub>1</sub>=7.14 mM) and two levels of phosphorus (P<sub>0</sub>=0.084 and P<sub>1</sub>=0.420 mM).

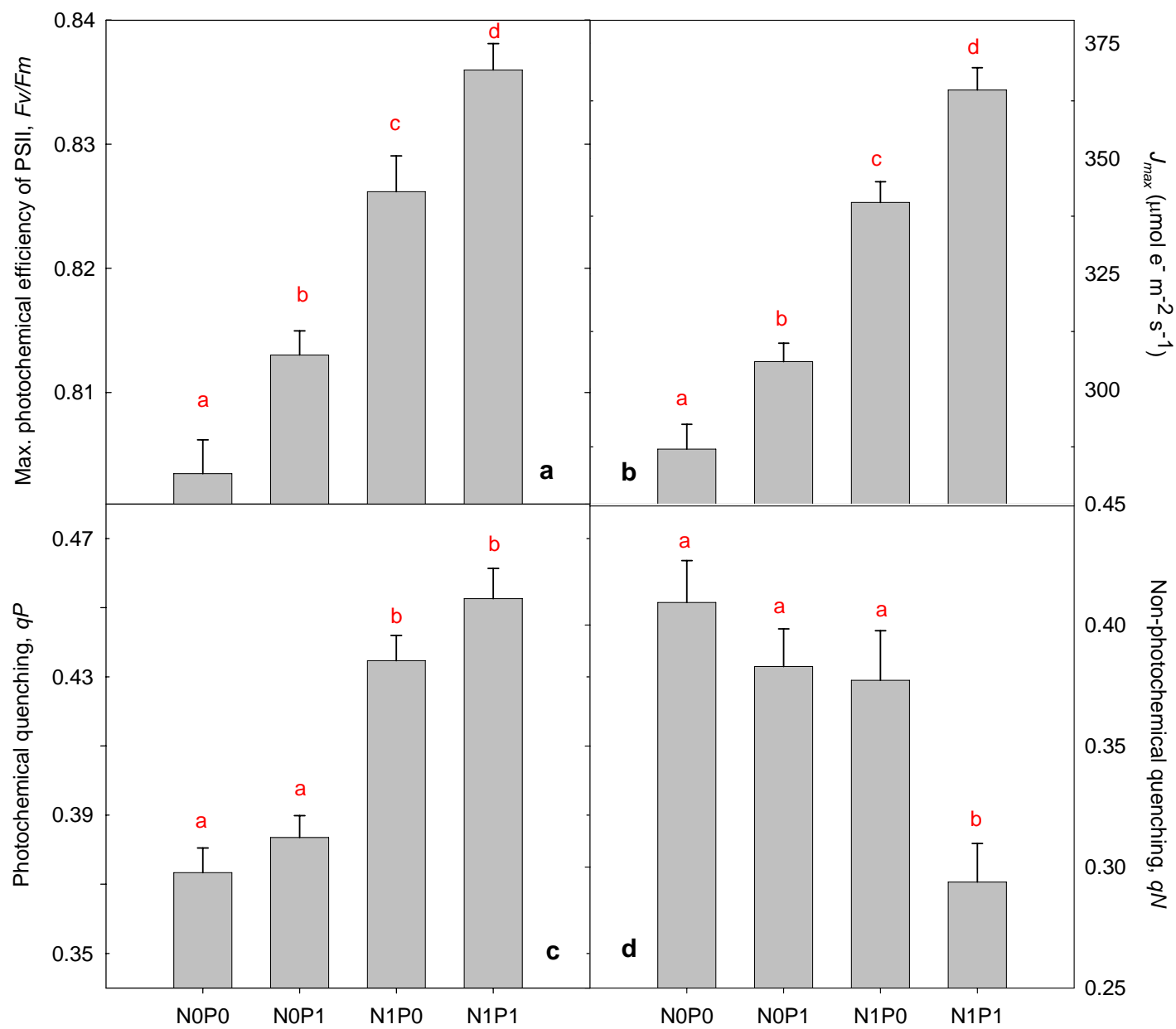


# Calvin cycle

- $V_{cmax}$ 
  - maximum carboxylation rate of Rubisco
  - Rubisco content
- $J_{max}$ 
  - Regeneration rate of RuBP
  - Thylakoid protein content







# Conclusion

- Research aimed at devising a nutritional modifier for hybrid models
    - Supply/Demand
  - Repeated Bray P analysis
  - C:N ratio
  - Step by step approach
    - Nutrient balance model
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